Phase transitions


## Gaseous State

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## GASEOUS STATE

The states of gases: Every substance has certain physical properties. The physical state of substance can be represented by its physical properties. These properties are related with each other and can be represented by a mathematical equation. The equation is called as equation of state. For ideal gas equation of state can be given as,

$$
\mathbf{P}=\frac{n R T}{V}
$$

## Where, $\mathbf{P}=\mathbf{f}(\mathbf{n}, \mathbf{V}, \mathbf{T})$

' $\mathbf{P}$ ' is pressure which is defined as force divided by the area to which the force is applied.
' $T$ ' is temperature is the property that indicates the flow of energy through a thermally conducting rigid wall.
' V ' is volume and ' n ' is number of moles.

## POSTULATES OF KINETIC THEORY OF GASES

Kinetic theory of gases considers the atoms or molecules of a gas as a constantly moving point masses, with huge inter-particle distance and may undergo perfectly elastic collisions. Implications of these assumptions are i) Particles:

Gas is a collection of a large number of atoms or molecules. Properties of the individual are same as that of the gas as the whole.

ii) Point Masses:

Atoms or molecules making up the gas are very small particles like a point(dot) on a paper with a small mass.


## iii) Negligible Volume Particles:

Particles are generally far apart such that their inter-particle distance is much larger than the particle size and there is large free unoccupied space in the container.

Compared to the volume of the container, the volume of the particle is negligible (zero volume).


## iv) Nil Force of Interaction:

Particles are independent. They do not have any (attractive or repulsive) interactions among them.


## v) Particles in Motion:

The particles are always in constant motion. Because of lack of interactions and the free space available, the particles randomly move in all directions but in a straight line.

## vi) Volume of Gas:



Because of motion, gas particles, occupy the total volume of the container whether it is small or big and hence the volume of the container to be treated as the volume of the gases.


## vii) Mean Free Path

This is the average distance a particle travels to meet another particle.


## viii) Kinetic Energy of the Particle

Since the particles are always in motion, they have average kinetic energy (K.E $\alpha$ T) proportional to the temperature of the gas.


## ix) Constancy of Energy / Momentum

Moving particles may collide with other particle or container. But the collisions are perfectly elastic. Collisions do not change the energy or momentum of the particle.

Elastic Collisions

Elastic collision
Inelastic collision

## xi) Pressure of Gas:

Collision of the particles on the walls of the container exerts a force on the walls of the container. Force per unit area is the pressure. The pressure of the gas is thus proportional to the number of particles colliding (frequency of collisions) in unit time per unit area on the wall of the container.


FIGURE 15-2. If the volume of
a gas is halved, the number of collisions with the walls of the container doubles. Thus, the pressure in container (b) is twice that of container (a).

Kinetic gas equation:-

$>$ Consider a cubical container of length ' $l$ ',
$>$ filled with gas molecules each having mass ' $m$ '
$>$ Let ' $N$ 'be the total number of gas molecules in the container.
$>$ Due to the influence of temperature, the gas molecules move in random directions with a velocity 'v.'
> The pressure of the gas molecules is the force exerted by the gas molecule per unit area of the wall of the container and is given by the equation,

$$
\mathrm{P}=\frac{F}{A}
$$

$>$ Let us consider a gas molecule moving in the X -direction towards face ' A '.
$>$ The molecule hits the wall with a velocity $\mathrm{V}_{\mathrm{x}}$ and rebounds back with the same velocity

$$
V_{x},
$$

The momentum (p) of the molecule before it strikes surface,
$\square$ The momentum after impact/collision $=\mathbf{p}=\mathbf{m} .\left(-\mathbf{V}_{\mathbf{x}}\right.$
and thus experience a change of momentum due to one impact which is equal to

$$
\Delta p=-m V_{x}-\left(-m V_{x}\right)
$$

Therefore $\Delta \mathbf{p}=\mathbf{- 2 m} \mathbf{V}_{\mathbf{x}}$ By the law of conversation of momentum the momentum transferred by the molecule $\mathrm{A}_{1}$ to the wall will be,

$$
\Delta p=+2 m V_{x} \text {----------------------(1) }
$$

For a total of ' N ' number of gas molecules in the container, all such change in momentum is given by,

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\Deltap=-2NmVx(2)
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After the collision, the molecule travels a distance of ' $2 l$ ' before colliding again with wall ' 1 '.

Thus, the time taken is given by,

Time $=\frac{\text { Distance travelled }}{\text { Velocity }}$

$$
\begin{equation*}
\text { Therefore, } \text { Time }=\frac{2 l}{V_{x}} \tag{3}
\end{equation*}
$$

These continuous collisions carry a force, given by

$$
\begin{equation*}
F=\frac{\text { Change in momenum }(\Delta \mathbf{p})}{\text { change in time }(\Delta t)} \tag{4}
\end{equation*}
$$

Therefore, substituting the values from equation (3) and (4), we get

$$
\begin{equation*}
F=\frac{-2 N m V x}{2 l / V x} \tag{5}
\end{equation*}
$$

Force exerted by ' $n$ ' number of molecules ${ }^{\prime} F^{\prime}=\frac{-\mathrm{NmV}^{2} \mathrm{x}}{1}$

$$
\begin{equation*}
{ }^{\prime} F^{\prime} \text { wall }=\frac{\mathrm{Nm}^{2} x}{l} \tag{6}
\end{equation*}
$$

But pressure is the force per unit area.
Pressure 'P'= Force on wall $(F)$ Area $(A) \quad$ so, $\quad$ Pressure $\boldsymbol{e}^{\prime} \boldsymbol{P}^{\prime}=\frac{N m V^{2} x / \boldsymbol{l}}{l^{2}}$
$\operatorname{Pressure}^{\prime} \mathrm{P}^{\prime}=\frac{N m V^{2} x}{l^{3}}$
Since $V_{x}, V_{y}$ and $V_{Z}$ are independent speed in three directions and if we consider the gas molecules in bulk, then $\mathrm{V}^{2} \mathrm{x}=\mathrm{V}^{2} \mathrm{y}=\mathrm{V}^{3} \mathrm{z}$

Hence, $\mathrm{V}^{2}=3 \mathrm{~V}^{2} \mathrm{x}$
Substituting the above condition in eq (9), we get,

$$
\mathbf{P V}=\frac{1}{3} m N V^{2}
$$

$$
P V=\frac{N m V^{2}}{3}
$$

This equation is known as the kinetic theory equation.

## Deduction of gas laws:

Boyle's law: _Under a constant temperature when the pressure on a gas increases its volume decreases. In other words according to Boyle's law volume is inversely proportional to pressure when the temperature and the number of molecules are constant.

## $\mathrm{V} \alpha 1 / \mathrm{P}$ at constant temp.

The K.E. of ' $n$ ' molecules are equal to $1 / 2 \mathrm{mnu}^{2}$
we knows that kinetic gas postulates K.E. is directly proportional to the temp.
Therefore,

$$
1 / 2 \mathrm{mnu}^{2} \alpha T
$$

$\mathbf{1 / 2} \mathbf{m n u}{ }^{2}=K T-------$ - (1) Where ' $K$ ' is proportionality constant.
Rewriting kinetic gas equation we get, $\mathbf{P V}=\mathbf{2 / 3}(\mathbf{1} / \mathbf{2}) \mathbf{m n u}^{\mathbf{2}}$
Therefore. $\mathbf{P V}=\mathbf{2 / 3 K T}--------\mathbf{- 1}^{(2)}$ Therefore PV= constant,
which is representation of Boyles law.

Charle's law: According to Charles law Volume is directly proportional to the temperature of gas V $\alpha \mathrm{T}$
Alternatively, at constant volume, pressure is directly proportional to temperature.
$\mathrm{P} \alpha \mathrm{T}$ (at constant V)
Rearranging equation (2) we get, $\mathrm{PV}=2 / 3 \mathrm{KT}$
Therefore V=2/3 K/P.T
at constant pressure, $\quad V=K^{\prime}$ 'T---------------(3) Where $K^{\prime}=\mathbf{2 / 3} \mathbf{K} / \mathbf{P}$
Therefore, $\mathrm{V} \alpha \mathrm{T}$ which is the representation of Charles law.
C) Avogadro's hypothesis: - According to Avogadro's "equal volumes of gases at the same temperature and pressure contain the same number of molecules".

Let us_consider two different gases. The kinetic gas equation can be written as, $\mathrm{P}_{1} \mathrm{~V}_{1}=1 / 3 \mathrm{~m}_{1} \mathrm{n}_{1} \mathrm{u}_{1}{ }^{2}$.
and $\mathrm{P}_{2} \mathrm{~V}_{2}=1 / 3 \mathrm{~m}_{2} \mathrm{n}_{2} \mathrm{u}_{2}{ }^{2}-\cdots---\cdots----(5)$ at constant temp. $\mathrm{P}_{1} \mathrm{~V}_{1}=\mathrm{P}_{2} \mathrm{~V}_{2}$

Therefore, $1 / 3 \mathrm{~m}_{1} \mathrm{n}_{1} \mathrm{u}_{1}{ }^{2}=1 / 3 \mathrm{~m}_{2} \mathrm{n}_{2} \mathrm{u}_{2}{ }^{2}$
If these two gases are at same temp., the kinetic energies of the molecules will be the same, that is,

$$
\begin{equation*}
1 / 3 \mathrm{~m}_{1} \mathbf{u}_{1}{ }^{2}=1 / 3 \mathrm{~m}_{2} \mathbf{u}_{2}^{2} . \tag{7}
\end{equation*}
$$

Substituting in equation (6) we get; $\mathbf{n}_{1}=\mathbf{n}_{2}$
Hence Avogadro's law has been deduced.
Grahams Law of diffusion:- According to Graham's " at constant temperature and pressure the rates of diffusion of various gases are inversely proportional to the square roots of their densities or molecular weights"
$\mathbf{R}$ (Rate of diffusion) $\boldsymbol{\alpha} \frac{1}{\sqrt{\mathrm{~d}}} \quad$ or $\frac{\sqrt{u_{1}}}{\sqrt{u_{2}}}=\frac{\sqrt{\rho_{2}}}{\sqrt{\rho_{1}}}=\frac{\sqrt{m_{2}}}{\sqrt{m_{1}}}$
Consider equation (6).......

$$
1 / 3 \mathrm{~m}_{1} \mathrm{n}_{1} \mathrm{u}_{1}^{2}=1 / 3 \mathrm{~m}_{2} \mathrm{n}_{2} \mathrm{u}_{2}^{2}
$$

$$
\mathrm{u}_{1}{ }^{2} / \mathrm{u}_{2}^{2}=\mathrm{n}_{2} \mathrm{~m}_{2} / \mathrm{n}_{1} \mathrm{~m}_{1} \quad \text { if } \mathrm{n}_{1}=\mathrm{n}_{2}=\mathrm{N}
$$

then, $\mathrm{u}_{1}{ }^{2} / \mathrm{u}_{2}{ }^{2}=\mathrm{Nm}_{2} / \mathrm{Nm}_{1}=\mathrm{M}_{2} / \mathrm{M}_{1}$
but $\mathrm{M}_{1} / \mathrm{V}=\mathrm{d}_{1}$ and $\mathrm{M}_{2} / \mathrm{V}=\mathrm{d}_{2}$ therefore,

$$
\begin{equation*}
\mathbf{u}_{1}{ }^{2} / \mathbf{u}_{2}{ }^{2}=d_{1} / \mathbf{d}_{2} \tag{8}
\end{equation*}
$$

Deviation from ideal behavior: - Ideal gas obeys the gas laws for all values of pressure and temp.,in reality, all gases obey the gas laws only over a range of pressure and temp. and not for all values of pressure and temp., hence real gases can be described in terms of the deviations from the gas laws.

## Deviations from Boyle's law: -

> If we plot PV against ' P ', for an ideal gas should be straight line parallel to the X axis.
$>$ This indicates that for an ideal gas PV should remain constant at constant temp.
> For real gas, such a straight line will not obtain.
$>$ Gases like hydrogen, nitrogen shows positive deviations, for these gases product PV increases with increase in pressure.
> Some gases like methane and carbon dioxide show product PV is found to be decreases. Small deviations from the Boyles law are observed only to low pressures.


## Deviations from Charles law: -

For a given amount of gas at constant pressure the volume of a gas increases or decreases by $1 / 273$ times its volume at $0^{\circ} \mathrm{C}$, for every degree rise of fall in temperature.1/273 or 0.003661 is the temp. Coefficient of the gas.

This remains same for all gases for all range of pressure and temp.

## Reasons for the deviations from ideal behavior :-

$>$ Volume of gas molecules that is the actual volume occupied by the gas molecules is negligible in comparison with the volume available to them that is the volume of the container.
$>$ Therefore the actual volume of gas $=$ Volume of container - Volume of the gas molecules.
> Molecules of the gas don't exert any force of attraction over one another. In reality molecules of real gases exerts force of attractions with each other, as distance between two molecules increases force of attraction increases. Hence deviations from the ideal behavior are expected at high pressure.
> K.E. of molecules increases, some of K.E.is used to overcome the intermolecular force, hence the gas behaves ideally, but as temp.is lowered, the average K.E. of gas molecule will decreased.it may not be sufficient to overcome the force of attraction. Hence, a deviation from ideality may be observed.

Vanderwaals equation of state: - $\left(p+\frac{n^{2} a}{\nu^{2}}\right)(v-n b)=$ nRт
$>$ It shows relation between all the variables at the given state is called equation of state.
$>$ For gases state ' P ', ' V ' ' T ' and ' n ' are variables that defines the states. $\mathrm{PV}=\mathrm{n}$ RT is also an equation of state, but this is not obeyed by real gases for all the values of pressure, volume and temperature.
$>$ Hence some parameters has to be taken into account to explain the behavior of real gas.
> There are two faulty assumptions of kinetic theory of gases these are,
A) the volume of gas molecules is negligible in comparison with volume occupied by them.
$>$ B) No intermolecular force of attraction is present in the gaseous state. Van-der Waals provided an equation of state that will be obeyed by all real gases, at all values of pressure and temperature.

## Critical phenomenon: PV isotherms of real gases:-

 Critical phenomenon:Boiling Point:
## Liquifiction:



When a liquid is heated in an open vessel, the vapor pressure of liquid increases. At its boiling point, vapor pressure becomes equal to atmospheric pressure.

## Liquification:

1) on decreasing the temperature of the gas.
2) Secondly by increasing the pressure of the


## Critical temperature

Critical pressure

## Critical volume

Interrelationships of above three....

> The ideal gas law assumes that a gas is composed of randomly moving, non-interacting point particles.(refer Postulates of kinetic theory of gases)
$>$ Real gases shows complex behavior that deviate from the ideal model.
> However as shown by graph (isotherms refers to the different curve so the graphs, which represent a gas state at different pressure and volume conditions but at constant temperature.)
$>$ Iso- means same and thermo means temperature-hence isotherm.
PV isotherms of real gases:- Critical phenomenon can be studied from PV curve curve expected to be hyperbola. The isotherms obtained at 40 atm . and above 40 atm. temperatures are hyperbolas.
$>$ At low temp. isotherms show inflection (change).e.g. At temp.31.04 deg. isotherm shows a point of inflection (point ' $\mathbf{P}$ 'in fig. 1 or point $\mathbf{E}$ in fig.2).The isotherm at temp. 13 deg. and 21.5 deg. Shows horizontal portion which represents no change of pressure for a large change in volume.
$>$ As temp.is increased, the flat portion of the isotherm is found to decrease in length until it converges into a single point at point 31.10 deg.
$>$ But when liquid is heated in a sealed tube, initially liquid and vapor will be in equilibrium.


Figure. Isotherms of Carbon
dioxide at different tempeartures

Conclusions from Graphical Study

$>$ On raising temp. more and more amount of the liquid will vaporize, hence, pressure inside tube increases.
> At every stage there is a line of demarcation (boundary) between the liquid and vapor phase.
> Critical Temp. or Critical point: At a particular temp. the liquid meniscus will disappear i.e. the line of separation between the two phases disappears and physical properties of the liquid and the gas become identical. This temp.is called critical temp. and the liquid is said to be at the critical point.('P'or'E')
$>$ On heating the tube further, no trace of the liquid can be found.
$>$ The total mass remains in the gaseous state even on increasing the pressure externally. Hence, it can be concluded that no liquid can exit at a temp. greater than its critical temp.


Figure. Isotherms of Carbon
dioxide at different tempeartures

Conclusions from Graphical Study


Isotherms of Carbon Dioxide at
Various Temperatures


## Thank you for your attention..

